

No calculators, charts or other extra material allowed.

Leave a few empty rows for grading notes at the top of the first page of your answer sheet.

- ~~1.~~ ~~(a)~~ Simplify $(\bigcup A) \cap (\bigcup B)$, where $A = \{\emptyset, \{\emptyset\}\}$ and $B = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}\}$.
~~(b)~~ Prove or disprove (i.e., provide a proof or a counter example): For any sets A and B

$$\mathcal{P}A \cup \mathcal{P}B = \mathcal{P}(A \cup B)$$

~~2.~~ Show that every natural number is a transitive set.

~~3.~~ Show that addition of reals is commutative, i.e.,

$$x +_{\mathbb{R}} y = y +_{\mathbb{R}} x$$

for all $x, y \in \mathbb{R}$. State without proof the results from earlier levels of the construction that you use in your proof.

4. Show that for any $n \in \omega$, any proper subset of n is equinumerous to some m less than n . (Hint: induction)